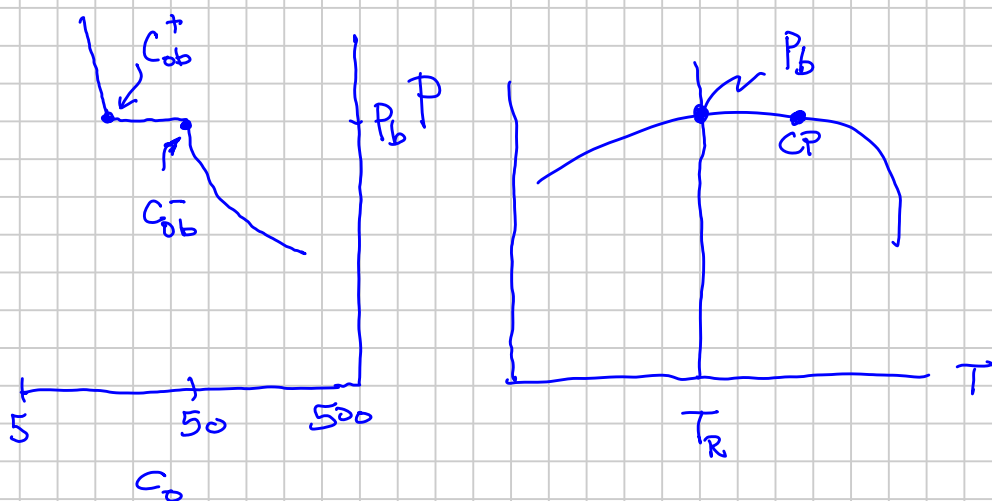


Isothermal Compressibility



Problem:
Henry Ramey
Hank

$$C_o \equiv -\frac{1}{V_o} \cdot \left(\frac{dV_o}{dp} \right)_T \approx \lim_{\Delta p \rightarrow 0} -\frac{1}{V_o} \frac{\Delta V_o}{\Delta p}$$

$C_{ob} @ P_b (T) ?$

$$\Delta V_o = V_o(p) - V_o(p - \Delta p)$$

$$\Delta p = p$$

$$\left(\frac{k}{\phi \mu c} \right)$$

$$\Delta p > 0 \quad P_b \rightarrow P_b + \Delta p > P_b$$

Single Phase
oil
↑

Single Phase
oil

Conventional
liquid
compressibility
 $\sim 5-50 \cdot 10^{-6} \frac{1}{psi}$

$$\Delta p < 0$$

$$P_b \rightarrow P_b - \Delta p < P_b$$

Two Phase

small gas
amount of
the volume

$$C_g \gg C_o$$

$$B_g = \frac{p_{sc}}{T_{sc}} \frac{T_R Z_g}{p} \propto \frac{1}{p}$$

$$b_g \propto p \quad \text{scf/ft}^3 \quad \text{Sm}^3/\text{m}^3$$

Initial Reservoir Gas Expansion Factor $b_{gi} \sim 50-300$

B_o

$b_o =$ "shrinkage factor" 5% - 300%

$$b_{oi} = 0.95 \quad 0.33$$

$$B_{oi} = 1.05 \quad 3-3.5$$

$$B_o(p, T) = \frac{V_o(p, T)}{V_o} \quad \begin{matrix} \swarrow \\ T_R \rightarrow T_{wh} \end{matrix}$$

Oil Formation Volume Factor "FVF" $T = T_R$

Oil Volume Factor @ any T

Gas-Oil Ratio GOR : R

Producing GOR : R_p

Solution GOR : R_s

property of a well

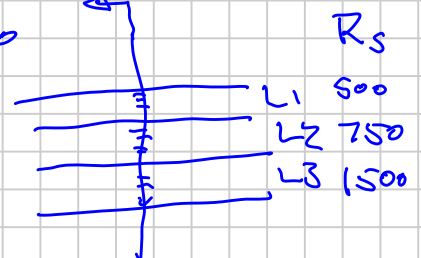
property of an oil

$$R_p = \begin{matrix} 600 \\ 1200 \end{matrix}$$

Oil-Gas Ratio OGR : $\frac{1}{R}$

CGR : $\frac{1}{R_p}$

$\frac{1}{R_s}$



Gas PVT Properties

Z_g (Z-factor) (Gas Deviation Factor)

$$pV = nRTZ_g$$

$$Z_g(T_{pr}, P_{pr})$$

$$T_{pr} \equiv \frac{T(R \text{ or } K)}{T_{pc}}$$

$$P_{pr} = \frac{P}{P_{pc}}$$

Getting P_{pc} & T_{pc} key!
 $f(y_i, C_2)$

$$\sim f(\gamma_g)$$

Reservoir GAD \Rightarrow use the reservoir gas MW_g to get γ_g

$$\rho_g = \frac{m}{V_g} = \frac{nM}{V_g} = \frac{pM_g}{RTZ_g}$$

Assume that producing wellstream \approx reservoir gas:

R depends on units

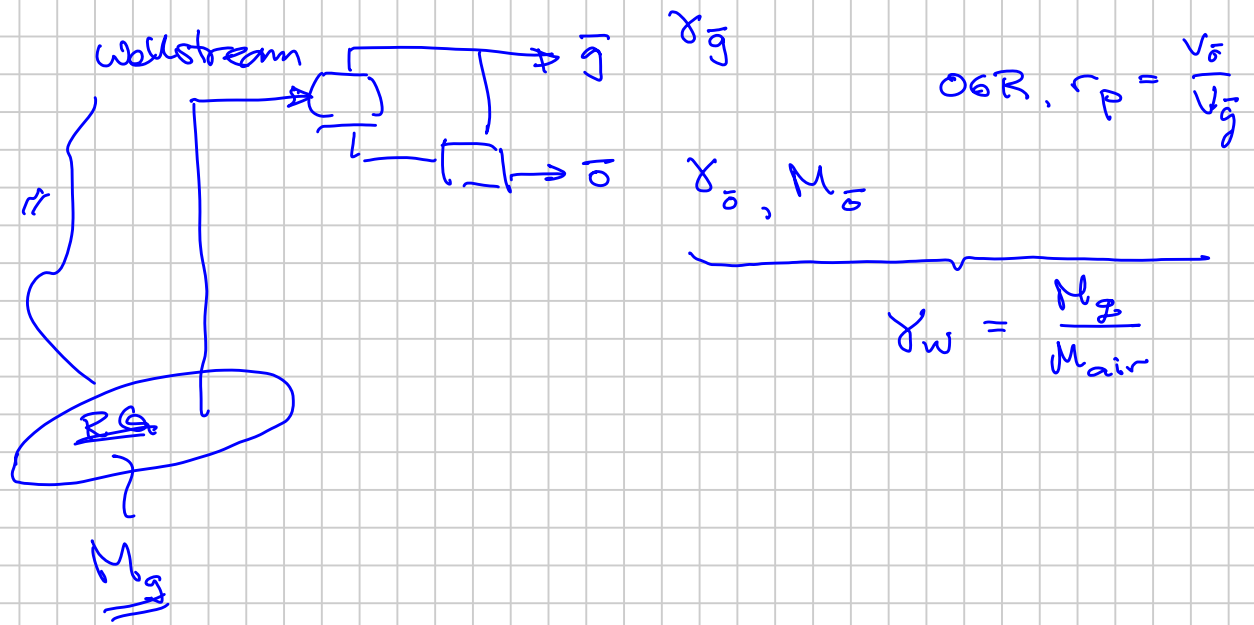
$\left. \begin{matrix} P \\ T \\ m \\ V \end{matrix} \right\}$ App. A

$$\underline{\gamma_w} = \frac{M_w}{M_{air}}$$

Eq. 3.38

$$\frac{V_{g(p,T)}}{V_g} = B_g = \frac{p_{sc}}{T_{sc}} \cdot \frac{T Z_g}{P}$$

Assumes that all of the gas at (p,T) becomes a surface gas - i.e., no surface oil condensing at surface



3.57 - 3.64 ignore for this course

Gas Viscosity: not measured
Lee-Gonzalez:

$$\mu_g (T, p_g, M_g)$$

Ignore the other gas viscosity correlations
in this course 3.66 - 3.68

Ignore Gas-0.1 Total FVF (3.3.7)

Gas-PVT e-note: Ex-1.xls

Oil PVT Properties:

Many many correlations

$$P_b = f(T, R_s, \gamma_o, \gamma_g)$$

± 2-20% accuracy

Standing

Glasø

$$R_s \leq 1500 \frac{\text{scf}}{\text{STB}}$$

$$AD \approx 20$$

$$T \approx 300^\circ\text{F}$$



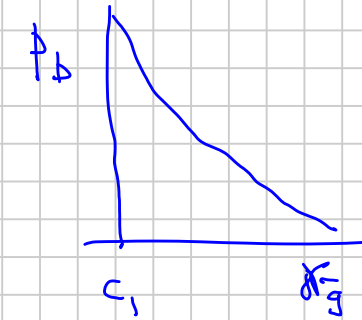
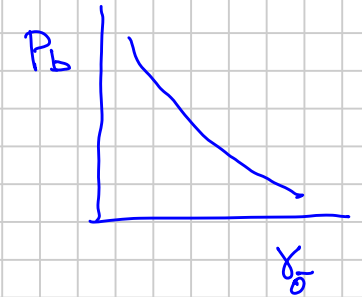
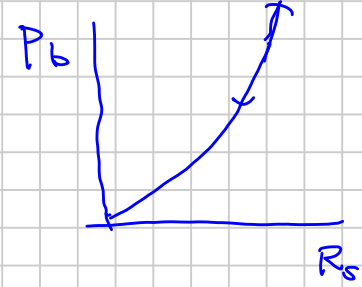
Appearance of Gas:

- Bad: $\Delta \downarrow$

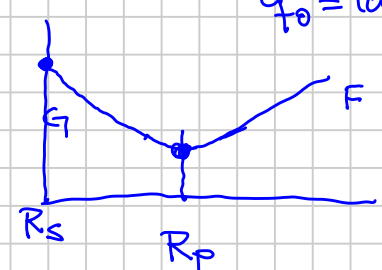
- Good: Improved Oil Recovery by Gas Segregation

Vertical Pipe Flow

$$q_o = 1000 \text{ SM}^3/\text{d}$$



$P_{wf} - P_{wh} \sim \Delta P_{\text{tubing}}$
function gravity



Matbakh
Prosper (Petroleum Experts)
Well Test SWP

When we two phases anywhere (g+o)

Eq. 3.78

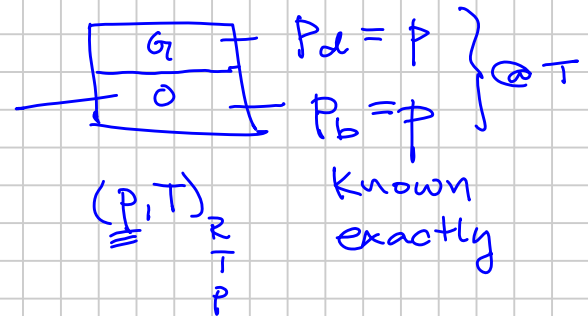
$$P_b = f(R_s, T, \gamma_o, \gamma_g)$$

invert

$$R_s = f(P_b, T, \gamma_o, \gamma_g)$$

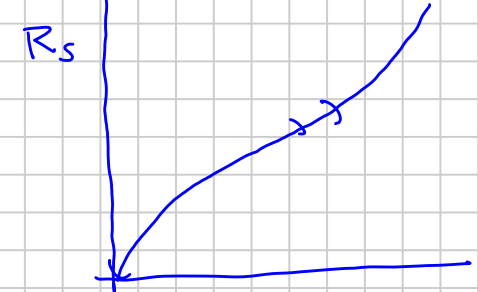
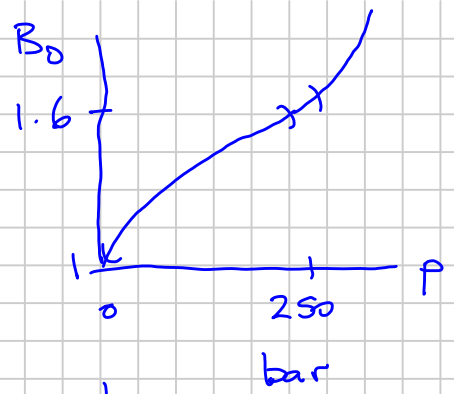
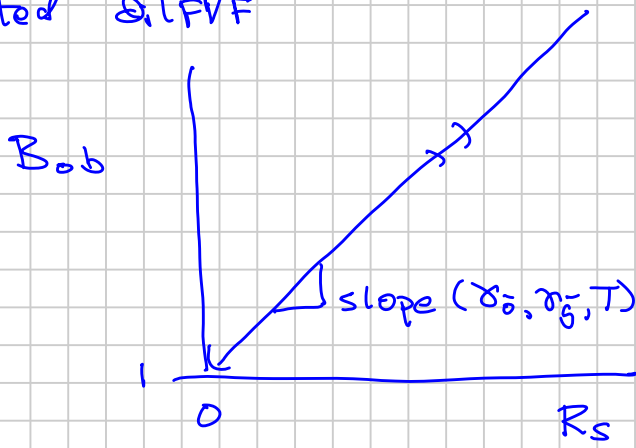
Eq. 3.87

Job (R_s, \dots)
Mo (R_s, \dots)
"R_s"
@ (P, T)²



$$B_{ob} : f(\underline{R}_s, \underline{\gamma}_o, \underline{\gamma}_g, \underline{T})$$

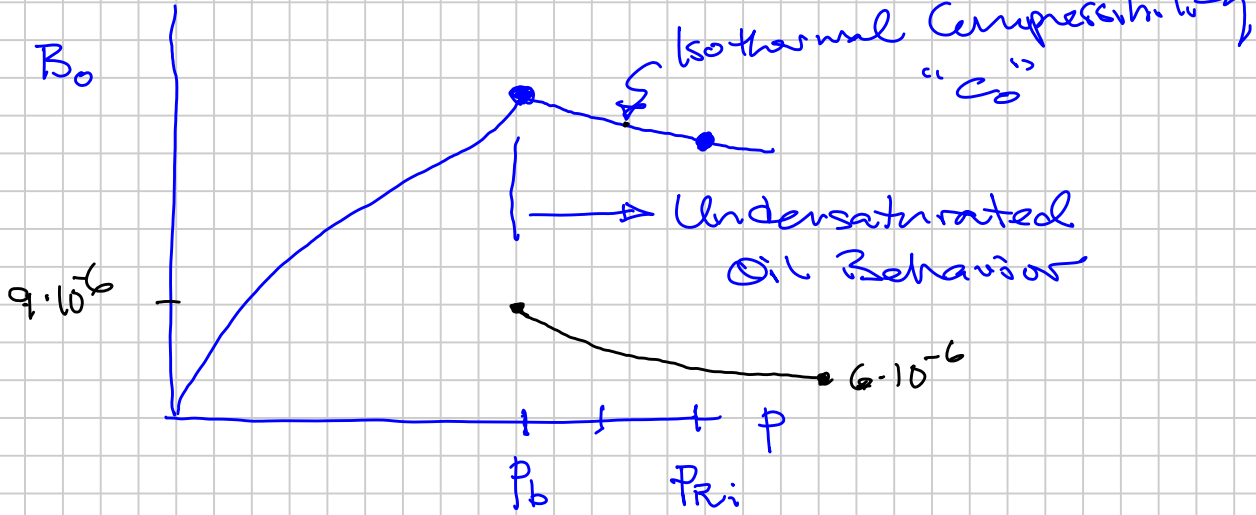
Saturated Oil PVF



$$\frac{1}{\rho} B_o (p > p_b)$$

$$R_s = 150 \text{ m}^3/\text{m}^3$$

$$\frac{V_o(p,T)}{V_o} = B_o$$



$$\left(\frac{dV_o}{V_o} \right) \left(\frac{1}{\text{psi}} \right) = \text{psi}^{-1} \text{ bar}^{-1}$$

$$\rho_o^{(p,T)} = \frac{\rho_o + R_s \gamma_g \rho_{air,sc}}{B_o(p,T)} \quad \frac{m_o}{V_o} = \frac{m_o + m_g}{V_o}$$

metric (SI)

Basis: $V_o = 1 \text{ m}^3$

$$B_o = V_o / V_o = V_o$$

$$m_o = V_o \cdot \rho_o = \rho_o$$

$$m_g = V_g \cdot \rho_g$$

$$V_g = R_s \cdot V_o = R_s$$

$$\rho_g = \rho_{air,sc} \cdot \gamma_g$$

Gas Phase

$$\rho_g = \frac{P M_g}{RT Z_g}$$

Black-Oil PVT: B_g r_s

$$\left[\rho_g^{(P,T)} = \frac{\rho_g + \rho_o r_s(P,T)}{B_g(P,T)} \right] = \frac{m_g}{V_g} = \frac{m_g + m_o}{V_g}$$

"special" B_g

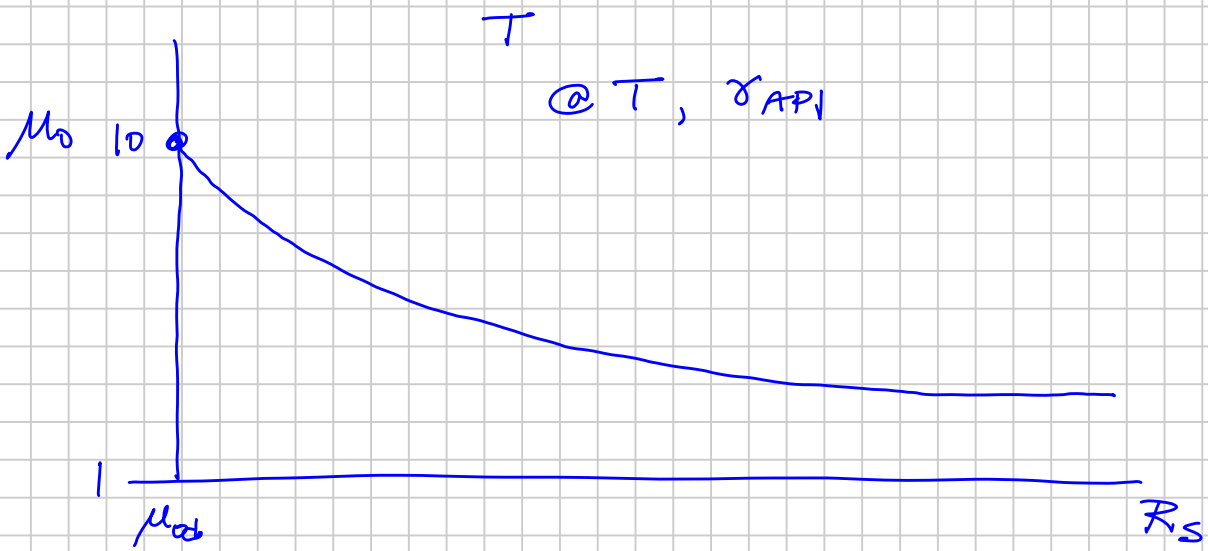
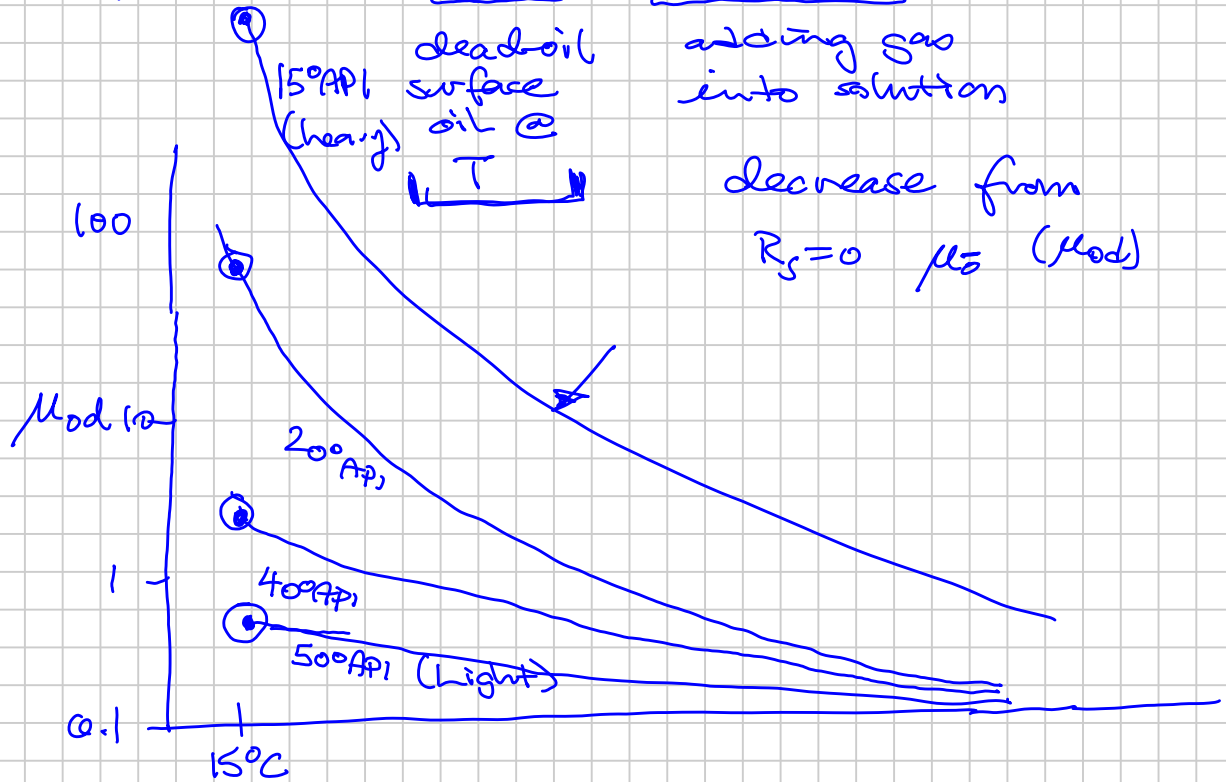
$$\Rightarrow \text{not } B_g = \frac{P_{sc}}{P} \frac{T Z}{T_{sc} Z_{sc}}$$

① μ_{ob}
 $\neq \mu_o$

@ all pressures $p > p_b$

$\mu_{ob}(T)$

$\mu_{ob}(T, p_b) = f(\underbrace{\mu_o(T)}, \underbrace{R_s(T, p_b)})$



$\mu_{oi} @ T_R$	
0.1 cp	} North Sea
10 cp	
10,000 cp	} Venezuela Canada

